



ALBA MATHEMATICS
Course Revision Questions
Task Sheet 8



1. A curve has equation $y = x^3 + 2x - 4$.
 - (a) Show that the line $y = 2x + 4$ intersects the curve at the point (2,8).
 - (b) Show that there are no other points of intersection between the curve and the line.
2. The roots of $mx^2 + 4mx + 16 = 0$ are equal. Find the value of m .
3. Evaluate $\int_0^1 x^2 - 2x^{\frac{1}{2}} + 3 \, dx$
4. Solve $\frac{1}{2} \log_x 16 = 2$.
5. Prove that $\frac{\sin(A-B)}{\cos A \cos B} = \tan A - \tan B$
6. By writing 225° as $180^\circ + 45^\circ$, simplify $\sin 135^\circ + \cos 135^\circ$
7. The line with equation $x - 3y = k$ is a tangent to the circle with equation $x^2 + y^2 - 6x + 8y + 15 = 0$. Find the possible value(s) of k .
8. A function f exists where $f(x) = \frac{1}{4}(3x + 1)$.
 - a) Find the inverse of this function $f^{-1}(x)$.
 - b) Hence evaluate $f^{-1}(4)$
9. Sketch the graphs of $y = \sin 2x$ and $y = \sin(2x + \frac{\pi}{3})$ for $0 \leq x \leq 2\pi$.
10. The vectors $\mathbf{a} = 2\mathbf{i} + 3\mathbf{j} - \mathbf{k}$ and $\mathbf{b} = 3\mathbf{i} - \mathbf{j} + x\mathbf{k}$ are perpendicular. Find the value of x .